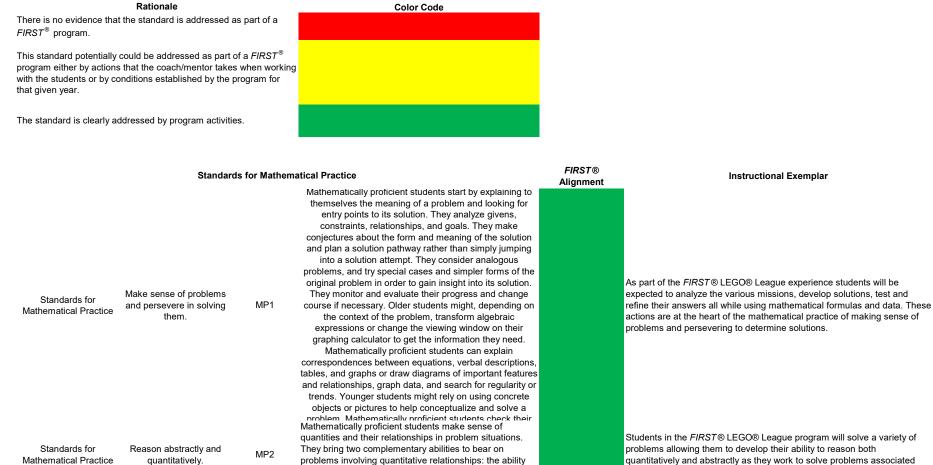
FIRST[®] LEGO[®] League Common Core Mathematics Standards Alignment & Instructional Exemplars



to decontextualize-to abstract a given situation and

represent it symbolically and manipulate the representing

with designing, building and programming their robot.

Standards for
Mathematical Practice

Construct viable arguments and critique the reasoning of others.

MP3

Standards for Model with mathematics. MP4

Standards for Mathematical Practice Use appropriate tools strategically.

MP5

mathematically proficient students understand and use stated assumptions, definitions, and previously established results in constructing arguments. They make conjectures and build a logical progression of statements to explore the truth of their conjectures. They are able to analyze situations by breaking them into cases, and can recognize and use counterexamples. They justify their conclusions, communicate them to others, and respond to the arguments of others. They reason inductively about data, making plausible arguments that take into account the context from which the data arose. Mathematically proficient students are also able to compare the effectiveness of two plausible arguments, distinguish correct logic or reasoning from that which is flawed, and-if there is a flaw in an argument-explain what it is. Elementary students can construct arguments using concrete referents such as objects, drawings, diagrams, and actions. Such arguments can make sense and be correct, even though they are not generalized or made Mathematically proficient students can apply the mathematics they know to solve problems arising in everyday life, society, and the workplace. In early grades, this might be as simple as writing an addition equation to describe a situation. In middle grades, a student might apply proportional reasoning to plan a school event or analyze a problem in the community. By high school, a student might use geometry to solve a design problem or use a function to describe how one quantity of interest depends on another. Mathematically proficient students who can apply what they know are comfortable making assumptions and approximations to simplify a complicated situation, realizing that these may need revision later. They are able to identify important quantities in a practical situation and map their relationships using such tools as diagrams, two-way tables, graphs, flowcharts and formulas. They can analyze those relationships mathematically to draw Mathematically proticient students consider the available tools when solving a mathematical problem. These tools might include pencil and paper, concrete models, a ruler, a protractor, a calculator, a spreadsheet, a computer algebra system, a statistical package, or dynamic geometry software. Proficient students are sufficiently familiar with tools appropriate for their grade or course to make sound decisions about when each of these tools might be helpful, recognizing both the insight to be gained and their limitations. For example, mathematically proficient high school students analyze graphs of functions and solutions generated using a graphing calculator. They detect possible errors by strategically using estimation and other mathematical knowledge. When making mathematical models, they know that technology can enable them to visualize the results of varying assumptions, explore consequences, and compare predictions with data. Mathematically proficient students at various grade levels are able to identify relevant external mathematical resources, such as digital content located on a website and use them to nose or

Building off the first practice, students in the *FIRST*® LEGO® League program will interact with their peers and be expected to provide reasoned critique of solutions developed supported by evidence and viable arguments.

Students in the *FIRST*® LEGO® League program will use mathematics and mathematical tools (e.g., charts, graphs, tables) to create different models that inform choices they make about robot design and programming.

Students in the *FIRST*® LEGO® League program will use a variety of ageappropriate mathematical tools (e.g., charts, graphs, tables, calculators) to solve mathematical problems encountered as they work to program their robot and optimize their strategy to address the various missions.

Standards for Mathematical Practice	Attend to precision.	MP6	Mathematically proficient students try to communicate precisely to others. They try to use clear definitions in discussion with others and in their own reasoning. They state the meaning of the symbols they choose, including using the equal sign consistently and appropriately. They are careful about specifying units of measure, and labeling axes to clarify the correspondence with quantities in a problem. They calculate accurately and efficiently, express numerical answers with a degree of precision appropriate for the problem context. In the elementary grades, students give carefully formulated explanations to each other. By the time they reach high school they have learned to examine claims and make explicit use of definitions.		Students in the <i>FIRST</i> ILEGO League program in order to complete the missions in the most efficient manner possible will have to develop their mathematical precision as they program their robot to interact with the different mission structures as well as navigate the game board.
Standards for Mathematical Practice	Look for and make use of structure.	MP7	Mathematically proficient students look closely to discern a pattern or structure. Young students, for example, might notice that three and seven more is the same amount as seven and three more, or they may sort a collection of shapes according to how many sides the shapes have. Later, students will see 7 × 8 equals the well remembered $7 \times 5 + 7 \times 3$, in preparation for learning about the distributive property. In the expression $x2 + 9x + 14$, older students can see the 14 as 2×7 and the 9 as $2 + 7$. They recognize the significance of an existing line in a geometric figure and can use the strategy of drawing an auxiliary line for solving problems. They also can step back for an overview and shift perspective. They can see complicated things, such as some algebraic expressions, as single objects or as being composed of several objects. For example, they can see $5 - 3(x - y)2$ as 5 minus a positive number times a square and use that to realize that its value cannot be more than 5 for any real numbers x and y.		Students in the <i>FIRST</i> ® LEGO® League program will learn to recognize and use patterns to solve problems and missions. In particular, students will take advantage of the properties of different shapes when they build their robot, program its movements, and determine solutions for the different missions.
Standards for Mathematical Practice	Look for and express regularity in repeated reasoning.	MP8	Mathematically proficient students notice if calculations are repeated, and look both for general methods and for shortcuts. Upper elementary students might notice when dividing 25 by 11 that they are repeating the same calculations over and over again, and conclude they have a repeating decimal. By paying attention to the calculation of slope as they repeatedly check whether points are on the line through (1, 2) with slope 3, middle school students might abstract the equation $(y - 2)/(x - 1) = 3$. Noticing the regularity in the way terms cancel when expanding $(x - 1)(x + 1)$, $(x - 1)(x2 + x + 1)$, and $(x -$ 1)(x3 + x2 + x + 1) might lead them to the general formula for the sum of a geometric series. As they work to solve a problem, mathematically proficient students maintain oversight of the process, while attending to the details. They continually evaluate the reasonableness of their intermediate results.		Students in the <i>FIRST</i> I LEGO League program will be able to experience regularity in repeated reasoning as they program their robot to complete the different missions in the game.
Domain	Cluster	Standard	Indicator/Skill	FIRST® Alignment	Instructional Exemplar

Ratios and Proportional Relationships	Understand ratio concepts and use ratio reasoning to solve problems.	6.RP.A.1	Understand the concept of a ratio and use ratio language to describe a ratio relationship between two quantities. For example, "The ratio of wings to beaks in the bird house at the zoo was 2:1, because for every 2 wings there was 1 beak." "For every vote candidate A received, candidate C received nearly three votes."	During programming the robot to navigate the game board and complete missions, the students will need to use ratios to compare the relationships between different elements such as wheel rotation and distance traveled, distanced traveled and speed.
Ratios and Proportional Relationships	Understand ratio concepts and use ratio reasoning to solve problems.	6.RP.A.2	Understand the concept of a unit rate a/b associated with a ratio a:b with $b \neq 0$, and use rate language in the context of a ratio relationship. For example, "This recipe has a ratio of 3 cups of flour to 4 cups of sugar, so there is 3/4 cup of flour for each cup of sugar." "We paid \$75 for 15 hamburgers, which is a rate of \$5 per hamburger."1	During programming the robot to navigate the game board and complete missions, the students will need to use ratios to compare the relationships between different elements such as wheel rotation and distance traveled, distanced traveled and speed.
Ratios and Proportional Relationships	Understand ratio concepts and use ratio reasoning to solve problems.	6.RP.A.3.A	Use ratio and rate reasoning to solve real-world and mathematical problems, e.g., by reasoning about tables of equivalent ratios, tape diagrams, double number line diagrams, or equations. a. Make tables of equivalent ratios relating quantities with whole number measurements, find missing values in the tables, and plot the pairs of values on the coordinate plane. Use tables to compare ratios.	In order to correctly navigate the game board, students will need to collect data in order to program the robot. They may record the data in tables of equivalent ratios if they choose or if they are directed to do so.
Ratios and Proportional Relationships	Understand ratio concepts and use ratio reasoning to solve problems.	6.RP.A.3.B	Use ratio and rate reasoning to solve real-world and mathematical problems, e.g., by reasoning about tables of equivalent ratios, tape diagrams, double number line diagrams, or equations. b. Solve unit rate problems including those involving unit pricing and constant speed. For example, if it took 7 hours to mow 4 lawns, then at that rate, how many lawns could be mowed in 35 hours? At what rate were lawns being mowed?	During programming the robot to navigate the game board and complete missions, the students will use ratios to compare the speed of the robot and how quickly it can move around the board.
Ratios and Proportional Relationships	Understand ratio concepts and use ratio reasoning to solve problems.	6.RP.A.3.C	Use ratio and rate reasoning to solve real-world and mathematical problems, e.g., by reasoning about tables of equivalent ratios, tape diagrams, double number line diagrams, or equations. c. Find a percent of a quantity as a rate per 100 (e.g., 30% of a quantity means 30/100 times the quantity); solve problems involving finding the whole, given a part and the percent.	While evaluating their game strategy, students will have the opportunity to calculate percents to determine whether or not a particular strategy is successful.
Ratios and Proportional Relationships	Understand ratio concepts and use ratio reasoning to solve problems.	6.RP.A.3.D	Use ratio and rate reasoning to solve real-world and mathematical problems, e.g., by reasoning about tables of equivalent ratios, tape diagrams, double number line diagrams, or equations. d. Use ratio reasoning to convert measurement units; manipulate and transform units appropriately when multiplying or dividing	To accurately program the robot, students will have to use ratio reasoning to convert amongst measurement units in the English and Metric systems of measurement.

The Number System	Apply and extend previous understandings of multiplication and division to divide fractions by fractions.	6.NS.A	Interpret and compute quotients of fractions, and solve word problems involving division of fractions by fractions, e.g., by using visual fraction models and equations to represent the problem. For example, create a story context for $(2/3) \div (3/4)$ and use a visual fraction model to show the quotient; use the relationship between multiplication and division to explain that $(2/3) \div (3/4) = 8/9$ because 3/4 of 8/9 is 2/3. (In general, $(a/b) \div (c/d) = ad/by$.) How much chocolate will each person get if 3 people share 1/2 lb of chocolate equally? How many 3/4-cup servings are in 2/3 of a cup of yogurt? How wide is a rectangular strip of land with length 3/4 mi and area 1/2 square mi?	By asking students to determine the points they can earn by completing different tasks under a variety of conditions (e.g. if 1/2 of the tasks are completed each earning partial points) they will need to use the skill of dividing or multiplying fractions by fractions.
The Number System	Compute fluently with multi-digit numbers and find common factors and multiples.	6.NS.B.2	Fluently divide multi-digit numbers using the standard algorithm.	Throughout the process of robot construction and programming (e.g. determine the average time it takes the robot to complete each mission) students will be required to divide multi-digit numbers.
The Number System	Compute fluently with multi-digit numbers and find common factors and multiples.	6.NS.B.3	Fluently add, subtract, multiply, and divide multi-digit decimals using the standard algorithm for each operation.	Throughout the process of robot construction and programming (e.g. determine the average time it takes the robot to complete each mission) students will be required to different mathematical operations.
The Number System	Compute fluently with multi-digit numbers and find common factors and multiples.	6.NS.B.4	Find the greatest common factor of two whole numbers less than or equal to 100 and the least common multiple of two whole numbers less than or equal to 12. Use the distributive property to express a sum of two whole numbers 1–100 with a common factor as a multiple of a sum of two whole numbers with no common factor. For example, express $36 + 8$ as $4 (9 + 2)$.	If the coach/mentor chooses, students may factor numbers to simplify calculations or to create values to be used in programming.
The Number System	Apply and extend previous understandings of numbers to the system of rational numbers.	6.NS.C.5	Understand that positive and negative numbers are used together to describe quantities having opposite directions or values (e.g., temperature above/below zero, elevation above/below sea level, credits/debits, positive/negative electric charge); use positive and negative numbers to represent quantities in real-world contexts, explaining the meaning of 0 in each situation.	During programming of the robot, students will be able to observe positive and negative numbers used to illustrate movement of the robot in opposite directions.
The Number System	Apply and extend previous understandings of numbers to the system of rational numbers.	6.NS.C.6.A	Understand a rational number as a point on the number line. Extend number line diagrams and coordinate axes familiar from previous grades to represent points on the line and in the plane with negative number coordinates. a. Recognize opposite signs of numbers as indicating locations on opposite sides of 0 on the number line; recognize that the opposite of the opposite of a number is the number itself, e.g., $-(-3) = 3$, and that 0 is its own opposite.	During programming of the robot, students will be able to observe positive and negative numbers used to illustrate opposite directions around a common point (e.g., 0).

The Number System	Apply and extend previous understandings of numbers to the system of rational numbers.	6.NS.C.6.B	Understand a rational number as a point on the number line. Extend number line diagrams and coordinate axes familiar from previous grades to represent points on the line and in the plane with negative number coordinates. b. Understand signs of numbers in ordered pairs as indicating locations in quadrants of the coordinate plane; recognize that when two ordered pairs differ only by signs, the locations of the points are related by reflections across one or both axes.	During programming of the robot, students will be able to observe positive and negative numbers used to illustrate movement around a common point (0, 0). Robot movement could be used to illustrate a coordinate plane and quadrants.
The Number System	Apply and extend previous understandings of numbers to the system of rational numbers.	6.NS.C.6.C	Understand a rational number as a point on the number line. Extend number line diagrams and coordinate axes familiar from previous grades to represent points on the line and in the plane with negative number coordinates. c. Find and position integers and other rational numbers on a horizontal or vertical number line diagram; find and position pairs of integers and other rational numbers on a coordinate plane.	During programming of the robot, students will be able to observe positive and negative numbers used to illustrate movement around a common point (0, 0). Robot movement could be used to illustrate a coordinate plane and quadrants.
The Number System	Apply and extend previous understandings of numbers to the system of rational numbers.	6.NS.C.7.A	Understand ordering and absolute value of rational numbers. a. Interpret statements of inequality as statements about the relative position of two numbers on a number line diagram. For example, interpret $-3 > -7$ as a statement that -3 is located to the right of -7 on a number line oriented from left to right.	Not Applicable
The Number System	Apply and extend previous understandings of numbers to the system of rational numbers.	6.NS.C.7.B	Understand ordering and absolute value of rational numbers. b. Write, interpret, and explain statements of order for rational numbers in real-world contexts. For example, write $-3 ^{\circ}\text{C} > -7 ^{\circ}\text{C}$ to express the fact that $-3 ^{\circ}\text{C}$ is warmer than $-7 ^{\circ}\text{C}$. Understand ordering and absolute value of rational	Not Applicable
The Number System	Apply and extend previous understandings of numbers to the system of rational numbers.	6.NS.C.7.C	numbers. c. Understand the absolute value of a rational number as its distance from 0 on the number line; interpret absolute value as magnitude for a positive or negative quantity in a real-world situation. For example, for an account balance of -30 dollars, write -30 = 30 to describe the size of the debt in dollars.	Not Applicable
The Number System	Apply and extend previous understandings of numbers to the system of rational numbers.	6.NS.C.7.D	Understand ordering and absolute value of rational numbers. d. Distinguish comparisons of absolute value from statements about order. For example, recognize that an account balance less than –30 dollars represents a debt greater than 30 dollars.	Not Applicable

The Number System	Apply and extend previous understandings of numbers to the system of rational numbers.	6.NS.C.8	Solve real-world and mathematical problems by graphing points in all four quadrants of the coordinate plane. Include use of coordinates and absolute value to find distances between points with the same first coordinate or the same second coordinate. dollars represents a debt greater than 30 dollars.	As part of the programming process, students could use ordered pairs on a coordinate plane to represent mission locations and find the distances between the points.
Expressions and Equations	Apply and extend previous understandings of arithmetic to algebraic expressions.	6.EE.A.1	Write and evaluate numerical expressions involving whole number exponents.	Students could be asked to formalize mathematical calculations into equations with exponents when working with the mathematics of circles (wheel rotations) and programming loops.
Expressions and Equations	Apply and extend previous understandings of arithmetic to algebraic expressions.	6.EE.A.2.A	 Write, read, and evaluate expressions in which letters stand for numbers. a. Write expressions that record operations with numbers and with letters standing for numbers. For example, express the calculation "Subtract y from 5" as 5 – y. 	As part of the programming process students will develop equations that use variables so that they can determine input values for a wide range of conditions (e.g. distance equals speed over time)
Expressions and Equations	Apply and extend previous understandings of arithmetic to algebraic expressions.	6.EE.A.2.B	 Write, read, and evaluate expressions in which letters stand for numbers. b. Identify parts of an expression using mathematical terms (sum, term, product, factor, quotient, coefficient); view one or more parts of an expression as a single entity. For example, describe the expression 2 (8 + 7) as a product of two factors; view (8 + 7) as both a single entity and a sum of two terms. 	If the coach/mentor chooses, students can explain the equations they develop using appropriate mathematical terms.
Expressions and Equations	Apply and extend previous understandings of arithmetic to algebraic expressions.	6.EE.A.2.C	Write, read, and evaluate expressions in which letters stand for numbers. c. Evaluate expressions at specific values of their variables. Include expressions that arise from formulas used in real-world problems. Perform arithmetic operations, including those involving whole number exponents, in the conventional order when there are no parentheses to specify a particular order (Order of Operations). For example, use the formulas V = s ³ and A = 6 s ² to find the volume and surface area of a cube with sides of length s = 1/2.	To correctly program the robot, students will need to enter real-world measurements into their equations thereby generating values to enter into the computer.
Expressions and Equations	Apply and extend previous understandings of arithmetic to algebraic expressions.	6.EE.A.3	Apply the properties of operations to generate equivalent expressions. For example, apply the distributive property to the expression 3 (2 + x) to produce the equivalent expression 6 + 3x; apply the distributive property to the expression 24x + 18y to produce the equivalent expression 6 (4x + 3y); apply properties of operations to y + y + y to produce the equivalent expression 3y.	While comparing different programming options, students will have the opportunity to work with equivalent expressions and evaluate the appropriateness of each for their purposes. Students could be asked to formalize this work into identification of properties used.
Expressions and Equations	Apply and extend previous understandings of arithmetic to algebraic expressions.	6.EE.A.4	Identify when two expressions are equivalent (i.e., when the two expressions name the same number regardless of which value is substituted into them). For example, the expressions $y + y + y$ and 3y are equivalent because they name the same number regardless of which number y stands for.	While comparing different programming options, students will have the opportunity to work with equivalent expressions and evaluate the appropriateness of each for their purposes.

Expressions and Equations	Reason about and solve one-variable equations and inequalities.	6.EE.B.5
Expressions and Equations	Reason about and solve one-variable equations and inequalities.	6.EE.B.6
Expressions and Equations	Reason about and solve one-variable equations and inequalities.	6.EE.B.7
Expressions and Equations	Reason about and solve one-variable equations and inequalities.	6.EE.B.8
Expressions and Equations	Represent and analyze quantitative relationships between dependent and independent variables.	6.EE.C.9
Geometry	Solve real-world and mathematical problems involving area, surface area, and volume.	6.G.A.1
Geometry	Solve real-world and mathematical problems involving area, surface area, and volume.	6.G.A.2
Geometry	Solve real-world and mathematical problems involving area, surface area, and volume.	6.G.A.3

Understand solving an equation or inequality as a process of answering a question: which values from a specified set, if any, make the equation or inequality true? Use substitution to determine whether a given number in a specified set makes an equation or inequality true.

Use variables to represent numbers and write expressions when solving a real-world or mathematical problem; understand that a variable can represent an unknown number, or, depending on the purpose at hand, any number in a specified set. Solve real-world and mathematical problems by writing and solving equations of the form x + p = q and px = q for cases in which p, q and x are all nonnegative rational numbers.

Write an inequality of the form x > c or x < c to represent a constraint or condition in a real-world or mathematical problem. Recognize that inequalities of the form x > c or x < c have infinitely many solutions; represent solutions of such inequalities on number line diagrams.

Use variables to represent two quantities in a real-world problem that change in relationship to one another; write an equation to express one quantity, thought of as the dependent variable, in terms of the other quantity, thought of as the independent variable. Analyze the relationship between the dependent and independent variables using graphs and tables, and relate these to the equation. For example, in a problem involving motion at constant speed, list and graph ordered pairs of distances and times, and write the equation d = 65t to represent the relationship between distance and time.

Find the area of right triangles, other triangles, special quadrilaterals, and polygons by composing into rectangles or decomposing into triangles and other shapes; apply these techniques in the context of solving real-world and mathematical problems.

Find the volume of a right rectangular prism with fractional edge lengths by packing it with unit cubes of the appropriate unit fraction edge lengths, and show that the volume is the same as would be found by multiplying the edge lengths of the prism. Apply the formulas V = I wh and V = b h to find volumes of right rectangular prisms with fractional edge lengths in the context of solving real-world and mathematical problems.

Draw polygons in the coordinate plane given coordinates for the vertices; use coordinates to find the length of a side joining points with the same first coordinate or the same second coordinate. Apply these techniques in the context of solving real-world and mathematical problems. To evaluate the performance of the robot and their programming strategy, students will compare the relationship between dependent and independent variables (e.g. time between missions = distance between missions divided by speed; where distance between is a set value).

While programming the robot, students will use solve real-world problems using a variable to represent a number that can vary depending upon conditions.

While programming the robot, students will use solve real-world problems using a variable to represent a number that can vary depending upon conditions.

While programming the robot, students will use inequalities to evaluate the relationships between variables that can have a wide range of real-world values (e.g., wheel-size, number of rotations).

To evaluate the performance of the robot and their programming strategy, students will compare the relationship between dependent and independent variables (e.g. time between missions = distance between missions divided by speed; where distance between is a set value).

During the process of building the robot, students can investigate the strength of using different shapes in their design and could be directed to find the area of these shapes as well.

Not Applicable

To determine distances that the robot will travel, students can be directed to use polygons they create on the coordinate plane.

Geometry	Solve real-world and mathematical problems involving area, surface area, and volume.	6.G.A.4	Represent three-dimensional figures using nets made up of rectangles and triangles, and use the nets to find the surface area of these figures. Apply these techniques in the context of solving real-world and mathematical problems.	Not Applicable
Statistics and Probability	Develop understanding of statistical variability.	6.SP.A.1	Recognize a statistical question as one that anticipates variability in the data related to the question and accounts for it in the answers. For example, "How old am I?" is not a statistical question, but "How old are the students in my school?" is a statistical question because one anticipates variability in students' ages.	Students will need to use statistics in determining the reliability of their robot and attachments in completing missions. Game strategy for completing missions require students to collect the results of practice attempts. Challenges may require investigation of data and statistics to provide support for the innovative solution proposed by students.
Statistics and Probability	Develop understanding of statistical variability.	6.SP.A.2	Understand that a set of data collected to answer a statistical question has a distribution which can be described by its center, spread, and overall shape. Recognize that a measure of center for a numerical data	If students collect the results of practice attempts to complete certain missions, they will have to opportunity to evaluate the distribution of the data.
Statistics and Probability	Develop understanding of statistical variability.	6.SP.A.3	set summarizes all of its values with a single number, while a measure of variation describes how its values	If students collect the results of practice attempts, they will have the opportunity to evaluate the meaning of the center of the data.
Statistics and Probability	Summarize and describe distributions.	6.SP.B.4	vary with a single number. Display numerical data in plots on a number line, including dot plots, histograms, and box plots. Summarize numerical data sets in relation to their	If students collect the results of practice attempts, they will have data that they can plot to evaluate its meaning.
Statistics and Probability	Summarize and describe distributions.	6.SP.B.5.A	context, such as by: a. Reporting the number of observations.	If students collect the results of practice attempts, they will have the opportunity to evaluate the number of observations recorded.
Statistics and Probability	Summarize and describe distributions.	6.SP.B.5.B	Summarize numerical data sets in relation to their context, such as by: b. Describing the nature of the attribute under investigation, including how it was measured and its units of measurement. Summarize numerical data sets in relation to their context, such as by:	If the coach/mentor chooses, students can discuss the concept being measured, how it was measured, and appropriate units.
Statistics and Probability	Summarize and describe distributions.	6.SP.B.5.C	c. Giving quantitative measures of center (median and/or mean) and variability (interquartile range and/or mean absolute deviation), as well as describing any overall pattern and any striking deviations from the overall pattern with reference to the context in which the data were gathered.	If students collect data about practice attempts, students will have the opportunity to evaluate the meaning of the median or mode as well the impact that the range of variability has on their strategies and programming.
Statistics and Probability	Summarize and describe distributions.	6.SP.B.5.D	Summarize numerical data sets in relation to their context, such as by: d. Relating the choice of measures of center and variability to the shape of the data distribution and the context in which the data were gathered.	Not Applicable